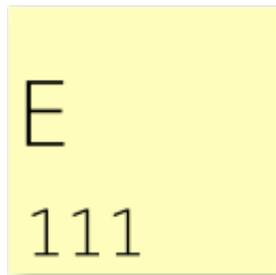
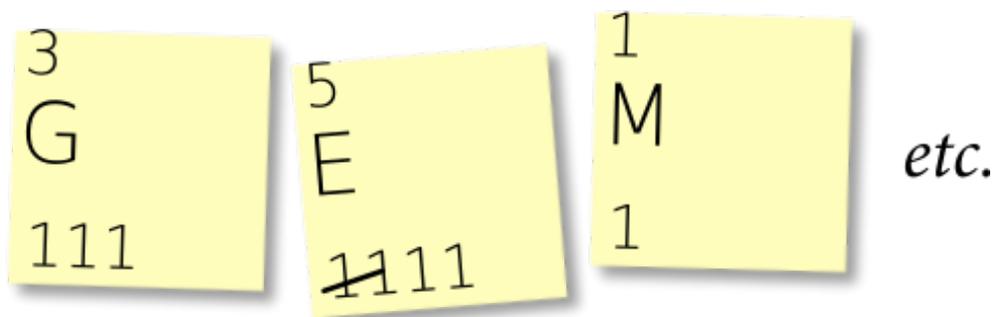


Move on to the next character in your message. Assuming it is a different character, make a new sticky for that one.

When you encounter a character that you've seen before, do **not** create a new note, but instead update the tally on the existing note containing that character. In this example, we've just seen the character E for the third time:



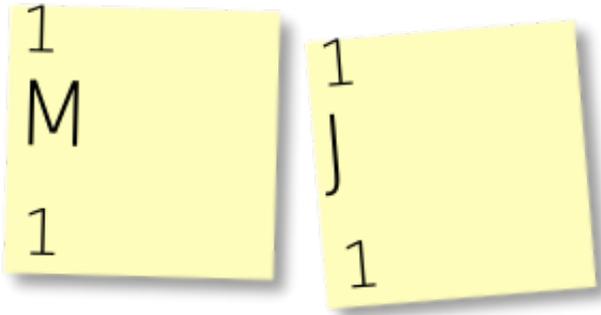
Continue doing this for the entire length of your message. You will now have a count of the frequencies of each character. Write the frequency in conventional (base ten) notation in the upper left. Here's a small sample:



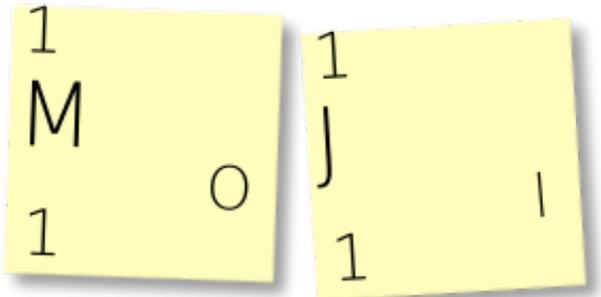
In the next section, we will process these characters in order from lowest frequency to highest. So you may want to take a moment now to arrange them in roughly that order on your desktop.

Phase 2: merge tiles

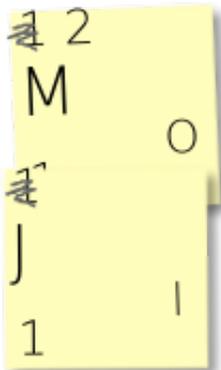
The algorithm continues by repeatedly merging sticky notes, as described here. Start by choosing two notes with the lowest frequencies. Probably you had several characters with a frequency of one, so you can just choose two of them arbitrarily. Place them side by side in your work area:



In the section beneath the character and **starting from the right**, write a zero on the left note and a one on the right note:



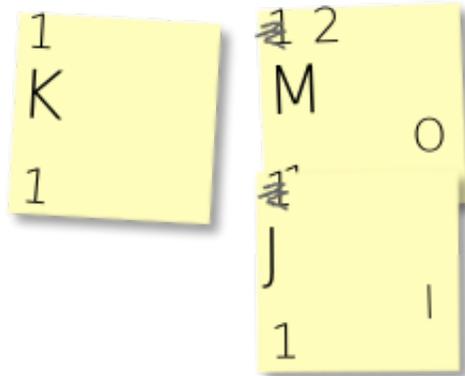
Then, stick the right one onto the bottom of the left one. Cross out the frequencies and replace the top one with their **sum** – in this case, $1+1$ is 2:



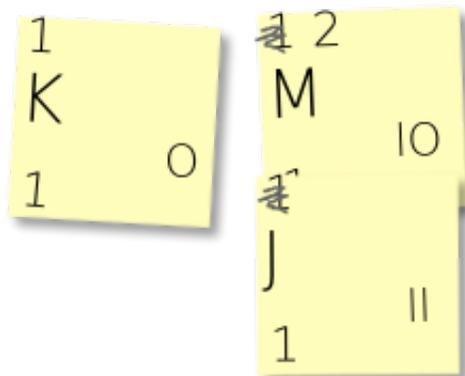
Now you will treat this 'merged' note as if it were a single one, so place it somewhere among other characters with frequency=2.

Continue merging together your lowest-frequency letters like this. It's okay to pair a frequency=1 with a frequency=2 if it's the last frequency=1 remaining – then the merged frequency would be 3.

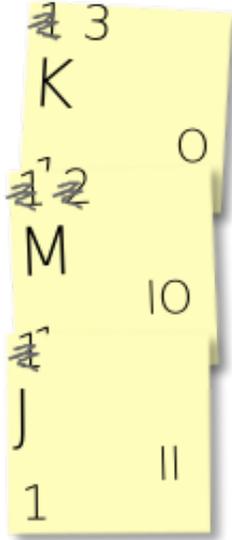
Before long, you'll have to merge notes that themselves are already merged. In the example below, we paired the last frequency=1 character (**K**) with a group (**MJ**) that has frequency=2:



As before, we write a zero on the left note. And we write ones on **all** of the right notes... to the left of whatever code is already there:



Again, stick the right note onto the bottom of the left one. Cross out the frequencies and replace the top one with their **sum** – in this case, $1+2$ is 3.



Continue merging notes using this technique until every character in your message is merged into one big note. Then you will have a distinct binary encoding underneath each character. Probably you should take a photo of your encoding, and/or write down the bits produced for each character elsewhere.

Visualize encoding as a tree

As in the handout on [variable-bit Huffman encoding](#), the character encodings you produced should fit nicely into a binary tree. I'll do a small example below. Our algorithm has produced the encodings 00 for K, 010 for M, 011 for J, and 1 for E.

We interpret a 0 as choosing the **left** path in a binary tree, and 1 as the **right** path. So to get to the K from the root we would go left, twice. For the E, we go right just once. The M and J both have the prefix 01, so they sit at a “sub-tree” reached by going left then right.

~~1000~~ 8
K 00
~~1010~~
M 010
~~1011~~
J 011
E
~~1111~~ 1

