Practice midterm solutions

26 October 2016

You have up to 1 hour, 45 minutes. You may use a calculator, but no text book or notes.

- 1. For each statement below, fill in the blank with the *best* term from the following list. Some terms might be used more than once; some might not be used at all.
 - algorithm ASCII binary bit Boolean byte compression CPU
 - hexadecimal input lossless lossy octal output pixel resolution
 - tree two's complement Unicode
 - (a) <u>resolution</u> refers to the number of pixels in a display or an image, or sometimes to the *density* of pixels in the display.
 - (b) <u>hexadecimal</u> is the name of a numbering system in which each digit corresponds to exactly four bits.
 - (c) <u>lossy</u> describes a type of compression in which the original data cannot be recovered with complete accuracy.
 - (d) <u>input</u> describes a device in the von Neumann architecture that provides data to the CPU.
 - (e) binary is the name we use for the base-two numbering system.
- 2. Write down the decimal (base 10) equivalents for the following 6-bit signed (two's complement) binary numbers. (That means the answers might be negative!)

The values of the columns in 6-bit two's complement are -32, 16, 8, 4, 2, 1.

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1 1 0 0 1 0 = <u>-32+16+2=-14</u> 1 1 1 1 0 1 = <u>-32+16+8+4+1=-3</u>

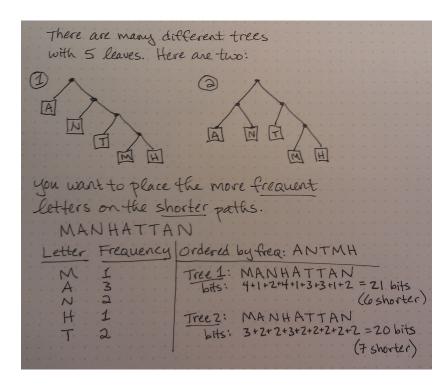
1 1 0 1 1 0 = <u>-32+16+4+2=-10</u> 0 1 0 0 0 1 = <u>16+1=+17</u>

0 0 0 1 0 1 = <u>4+1=+5</u> 1 1 1 1 1 1 = <u>-32+16+8+4+2+1=-1</u>
```

3. Add the following pairs of 5-bit signed (two's complement) binary numbers. Your answers must be in binary, but you should check your work by converting to decimal. Remember, values can be negative!

The values of the columns are -16, 8, 4, 2, 1. Remember the number circle, 4+12 is -16 because there's no way to represent +16 in 5-bit two's complement, and instead we *overflow* from positive numbers into the negative ones. A similar effect happens with -10+-15, only this time there's an extra carry bit that gets thrown away because it doesn't fit into the 5-bit answer.

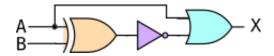
- 4. Suppose we want to design encodings just for the five letters A, H, M, N, and T.
 - (a) How many bits would we need to represent each letter in a **fixed-width** encoding? 3, because $2^3 = 8$ is enough letters.
 - (b) Using the fixed-width encoding in the previous question, how many bits would we need to represent the nine-letter word MANHATTAN? 27 = 9 letters \times 3 bits per letter
 - (c) Draw a tree to represent a **variable-width** encoding of these five letters. Use your tree to encode the word MANHATTAN. How many bits did you need? _ How many bits did you *save*, compared to the fixed-width encoding? _



5. Create a truth table to show the value of $X' + (X \cdot Y)$ for all possible inputs of X and Y.

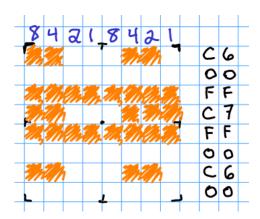
			Χ·Υ		
	+	+	+	 	_
0	0	1	0	1	
0	1	1	0	1	
1	0	0	0	0	
1	1	0	1	1	

6. Which Boolean expression is equivalent to the following circuit diagram?



- (a) $X = A' + (A \oplus B)$
- (b) $X = A + (A \oplus B)'$ (This one)
- (c) $X = A \oplus (A + B)'$
- (d) $X = A + (A \oplus B')$

7. Decode the following hexadecimal notation into an 8×8 icon, using 1 bit per pixel.



8. Convert the following binary number into hexadecimal and octal.

1010111001100100

For hexadecimal, group it into fours starting from the right: (1 0 1 0) (1 1 1 0) (0 1 1 0) (0 1 0 0) 8 4 2 1 8 4 2 1 8 4 2 1

Answer: A E 6 4

For octal, group it into threes starting from the right:

(1) (0 1 0) (1 1 1) (0 0 1) (1 0 0) (1 0 0) 1 4 2 1 4 2 1 4 2 1 4 2 1

Answer: 1 2 7 1 4 4

9. It's important that the steps in an algorithm are **unambiguous**. What does that mean?

Unambiguous means that the instruction is clear, and has only one possible interpretation.

- 10. What is the output of the following algorithm? Remember to indicate clearly what is *output* and what is scratch work.
 - 1. Set N to 0
 - 2. Set K to 5
 - 3. If K > 10 then output N and stop.
 - 4. Set N to N + K
 - 5. Set K to K + 1
 - 6. Go back to step 3.

SCRATCH WORK

Step 1 2 3 4 5 6 3 4 5 6 3 4 5 6 3 4 5 6 3 4 5 6 3 4 5 6 3 4 5 6 3 4 5 6 3 N 0 5 11 18 26 35 45 Stop K 5 6 7 8 9 10 11

OUTPUT

45