

teaching people to CODE as much as it is about teaching people to THINK ... right?

Figure 1: @hmason on Twitter

Algorithms

It's a little tricky to define an algorithm, but informally we can use the term interchangeably with more well-known English words like **recipe** or **procedure**.

Definition: an **algorithm** is a finite sequence of unambiguous and effectively computable instructions that produce some intended result.

Let's explore some of those terms in more detail:

- **finite:** An algorithm must **terminate** at some point. If it might go on forever, then we might never achieve the intended result.
- sequence: The instructions are ordered first do this, then do that, etc. and the order must be followed to achieve the correct result. (As an aside, there are *parallel* algorithms, in which the instructions are only *partially* ordered. We'll ignore that distinction for now.)
- **unambiguous:** Each instruction must be specified **precisely**, so there can be no confusion as to what must be done. If multiple interpretations of the instruction are possible, it's not an algorithm.
- **computable:** Each instruction must specify some task that **can be performed**. This gets a little theoretical, but there are some types of problems that no computer can solve in finite time. For now, let's just take a simple example of an uncomputable instruction: "predict tonight's lottery numbers." Because the lottery is random, there's no procedure we can follow to reliably predict it.
- **result:** We develop an algorithm to produce some specific **answer**. It could be a solution to a math problem, a stream of output, a modification of values stored in the memory, or whatever.



Figure 2:

Notation

An algorithm is independent of the language or notation in which it is specified. The **binary search** algorithm can be written in Python or Java or Ruby, but they're all the same algorithm.

One notation sometimes used for algorithms is called **pseudo-code** (where **pseudo** of course means "false" or "fake"). Unlike real code in a programming language, pseudo-code cannot be executed directly by a computer. However, because it's based on English (with a little mathematical notation), it's easier for untrained humans to understand.

Below is an example of an algorithm, written in pseudo-code, that will compute the **factorial** of a given integer, **N**. (The factorial is the result of multiplying all the numbers between 1 and N, so factorial of 4 is $1 \times 2 \times 3 \times 4 = 24$.)

Algorithm: factorial

- 1. Let N be an integer > 0.
- 2. Let K be 1.
- 3. If N = 1 then output K and stop.
- 4. Set K to $K \times N$.
- 5. Set N to N–1.
- 6. Go back to step 3.

To understand this algorithm, we need to introduce the concept of a **variable** in programming. We use variables in mathematics too, but they're a little different. In mathematics, a variable is a name given to a value, like x=5. In programming, a variable is a name given to a **location in memory**, which in turn can hold a value. The difference is that the value in the memory can be **updated** at a later time.

Let's trace the algorithm. In step 1, we're allowed to specify the value of **N**, as long as it is bigger than zero. This is a kind of **input** instruction. Let's use 4, so that the algorithm computes the factorial of 4. In step 2, another variable **K** is named, but it's initial value is 1. Here's what that looks like:

Step 3 asks whether N=1. It does not, so we skip the rest of that instruction.

Step 4 updates a variable. We first compute the value of the expression: $K \times N = 1 \times 4 = 4$, and then we write that value to the box labeled K, replacing whatever was there before:





Ν	4	3	
Κ	1	4	

Figure 4:

Step 5 updates the other variable. We first compute the value of the expression: N-1 = 4-1 = 3, and then we write that result to the box labeled N, replacing whatever was there before:

Step 6 says to go back to step 3. In step 3, N is still not 1, so we continue with the two updates again. This time, $K \times N = 4 \times 3 = 12$, and N-1 = 3-1 = 2:

N is still not 1, so we go through once more, producing these values for the two variables:

This time N=1, so in step 3 we output K and stop. By following this algorithm, we just computed the factorial of 4:

Output: 24

By starting the same algorithm with a different value of N, we could have computed any factorial.

Another example

Here's an algorithm you can try tracing yourself.

Algorithm:

- 7. Let A, B be integers > 0.
- 8. If A = B then output A and stop.
- 9. If A < B then set B to B–A and go back to step 2.



Figure 5:



Figure 6:

10. Otherwise set A to A–B and go back to step 2.

I won't tell you what this algorithm produces, but try it starting with these values for A and B:

A: 35 B: 21

Then try these:

A: 28 B: 12

And finally these:

A: 14 B: 33

Do you see the pattern? What does the algorithm compute?

Sorting

One rich area of algorithms is **sorting** – putting things in some order, whether that's alphabetical, numerical, chronological, or by size. There are many different sorting algorithms with different strengths and weaknesses. These videos introduce a few of them.

See also:

Diagram for Batcher's 'bitonic' sort

Speed

Whenever we talk about the "speed" of an algorithm, we have to consider the **size of the input**. In fact, we're usually most concerned about how the size of the input *impacts* the running time, as that size *increases*. Maybe for sorting 8 elements, there



Figure 7:

isn't much difference. But when we increase that to 50 or 1,000, dramatic differences may emerge.

Below is a graph comparing the number of comparisons for selection vs. merge sort, and also showing the lines N^2 and $N \cdot \log_2(N)$, which are characterizations of these different approaches. You can see that the selection sort is somewhat less than N^2 , however, they do grow large in the same awful way.