

Assignment 6 solution

See [the video](#).

1. Unify(real -> t4, t5 -> (string -> int))

- Both arrow types, unify left/right sides
- Unify(real, t5)
 - {t5 = real}
- Unify(t4, string->int)
 - {t4 = string->int}
- real -> string -> int

2. Unify(t1 -> (t2 -> real), int -> (t3 list -> real))

- Both arrow types, unify left/right sides
- Unify(t1, int) {t1 = int}
- Unify(t2->real, t3 list->real)
 - Both arrow types
 - Unify(t2, t3 list) {t2 = t3 list}
 - Unify(real, real) SUCCEEDS
- int -> t3 list -> real

3. Unify((int list) list, t6 list)

- Both application/ID types, both are list
- Unify(int list, t6) {t6 = int list}
- int list list

4. Unify((t7 list * t8) * t8, (t9 * t10 list) * t9)

- Both cross types, unify left/right
- Unify(t7 list * t8, t9 * t10 list)
- Unify(t8, t9) {t8=t9}
- Unify(t7 list * t9, t9 * t10 list)
 - Both cross types, unify left/right
 - Unify(t7 list, t9) {t9 = t7 list}
 - Unify(t9, t10 list)
 - Unify(t7 list, t10 list) {t7 = t10}
- t10 list * t10 list * t10 list

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fun crow xs =
  if null xs then 1
  else hd xs * crow (tl xs)

crow : t20 -> t21
xs : t20
null : t8 list -> bool
Unify(t20, t8 list) { t20 = t8 list }

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crow : t8 list -> t21
xs : t8 list
Unify(t21, Int)

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crow : t8 list -> int
hd: t9 list -> t9
hd xs: {t9=t8} t8
op* {t8=int}

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crow : int list -> int

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fun down x = if x=0 then [] else x :: down (x-1)

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down: t30 -> t31
x : t30
x=0 therefore {t30=int}
down: int -> t31
x : int
[] : t11 list {t31 = t11 list}

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down: int -> t11 list
op:: t12 * t12 list -> t12 list
op::(x, down(x-1)) {t12 = int}
op::(x, down(x-1)) :: int list
Unify(t11 list, int list) {t11=in}

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down: int -> int list

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fun edgar n = crow (down n)

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edgar : t40 -> t41
n : t40

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down : int -> int list
down n {t40=int}
down n : int list
crow : int list -> int
unify(int list, int list) succeeds
unify(t41, int) {t41 = int}

edgar : int -> int
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